Biological DNA and RNA Helices as Antennae for Electromagnetic Communication

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In addition to the electrogenic micro-organisms, e.g. bacteria, that can be found in communities that are wired together in circuits carrying electrons in and out of biological cells, there are wireless connections between micro-organisms that pass information to one another at a distance in virtue of electromagnetic signals. One needs electromagnetic antennae to send or receive signals as they pass information back and forth between living micro-organisms. We here discuss the properties of DNA and RNA long polymer molecules regarding their utility as antennae. As well as emitting or absorbing radiation photons these antennae also emit and absorb phonons, i.e. acoustic signals. The coupling between sound waves and electromagnetic waves is very appreciable due to and described by biological piezoelectricity. Biological phases of condensed matter also exhibit chiral symmetry breaking, i.e. "handedness" symmetry breaking, between right and left handed electronic states. Describing two spin components (say up and down) times two chirality components (say left and right) ultimately requires four component electron wave functions as discovered by Dirac even if the electrons are moving at velocities much less than light speed. Coupled with the quasi-one dimensional nature of long polymer molecules this yields bound Bose condensed bound particle-hole pairs constituting a Tomonaga-Luttinger liquid similar in some ways to the Bardeen-Cooper-Schriefer Bose condensed bound electron pairs found in superconductors. One similarity is that transport weak links in the Bose condensate fluid flow yield Josephson effects described by a quantum pendulum, e.g. a sine Gordon field theory. The coherent phase in the Tomonaga-Luttinger liquid is the difference between the right and left handed electronic phases as first demonstrated by Coleman via the conversion of the massive Thirring model into a Josephson type pendulum model. The complete theory of wireless communications between biological organisms is only beginning to be developed. The basic DNA and RNA microbe antennae must be wired in nature as a coherent phased antenna array for appreciable communication bit-rates radiated through large distances. Finally, acoustic and/or radio frequency electromagnetic radiation carrying sufficient communication information should be of use medically as a possible alternative to chemical medicines and/or vaccines in the treatment of illness for a most recent example in the COVID-19 virus with its RNA internal antenna.

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I. INTRODUCTION

There is a substantial literature describing the long wavelength excitations of long chain organic polymer biomolecules by quantum field theories in one spatial dimension. The applications of quantum field theoretic statistical thermodynamics[1] to the biological mantra that proteins are fabricated and controlled by mathematical computational programs contained within DNA and RNA macro-molecules[2] has thus far still been limited. Ultimately the methods of quantum field theory should be applicable to medicinal practice such as the development of alternatives to standard vaccines applied to the maladies of some DNA molecules within bacteria and some RNA molecules within viruses. Our purpose is to provide some initial stages towards studying field theoretical models. Applications to the RNA of the COVID-19 virus would have some immediate importance.

The microscopic theory of the condensed matter physics that can be used for understanding forces in biological matter must be based on the quantum electrodynamic interaction in continuous media[3]. At the classical level, the Lagrangian method employed for describing photons and collective electromagnetic field configurations is fairly well known[4]. Field quantization follows the canonical rules. For weak excitations in long chain bio-molecules, the effective Lagrangians describe bosons computed by functionally integrating out Fermion electron interactions. Purely *electron charge transport* can then be described by boson fields of the effective Lagrangian employing topologically charged soliton excitations. The mathematical properties of such soliton solutions of the boson equations of motion are very well established[5]. In what follows we consider electronic charge transport along DNA and RNA long chain molecules responsible for inducing electromagnetic antenna processes wherein very low frequency radio and acoustic frequency phonons and photons^[6] can be emitted and absorbed[7].

For the case of bacteria, there exist electronic communications within large communities because within a single community different cells are biologically wired to one another and circuit electrons pass through the biological mesh wiring through cell walls. A single bacterium with one or more connection wires allowing electrons to pass across the cell wall is often called an *electrogenic bacterium*. Studies of electrogenic bacteria communities abound [9–12] and engineering applications are beginning. For example, one may produce chemical batteries with electromotive forces induced by bacteria [13]. However the electricity in this case is maintained by wiring some bacteria to other bacteria and/or by wiring bacteria to chemical cell electrode surfaces.

Of central interest in this work is the wireless electrodynamic connections between bacteria and/or viruses.

In wireless connections, information is emitted or detected in antennae that can radiate, respectively absorb, electrodynamic radiation from a distance. In particular, our purpose is to discuss the antennae emission and absorption properties of long DNA and RNA molecules. Since these long polymer molecules are quasi- one dimensional, the electrical currents that emit or absorb radiation photons may be adequately described by one dimensional quantum electrodynamic models and these shall be essential to our general approach. In addition to photon excitations in the DNA and RNA molecules, there exist boson mechanical phonon oscillations, i.e. acoustic vibrations. The *phonon-photon* interaction thereby describes a piezoelectric effect in DNA and RNA molecules that occurs due to the chiral or handedness symmetry breaking, of the helical molecues that are double stranded for DNA and single stranded for RNA. The symmetry breaking must thereby be included in the one spatial dimensional field theoretical models employed to describe biological piezoelectricity[14, 15]. Ultimately this requires Dirac electron matrices that have dimension four; i.e. two spin states times two chiral states. Employing one spatial dimensional Dirac spinors, these four states can be handled

two states at a computational time.

The notion of describing electron charged currents in one spatial dimensional models with boson fields is very well known and constitutes the physical basis of Tomonaga-Luttinger fermion liquid models[16–18]. A central physical point is that a locally conserved charge in a model in one space plus one time dimension obeys the local charge conservation law $\partial_{\mu}J^{\mu} = 0$. In field theories with one spatial dimension

$$\frac{\partial \lambda(z,t)}{\partial t} + \frac{\partial I(z,t)}{\partial z} = 0, \qquad (1)$$

wherein $\lambda(z,t)$ and I(z,t) represent, respectively, the charge density per unit length and the current. For the problem of wireless communications between different DNA or RNA long polymer helical molecules, I represents the antennae current along the molecule emitting and absorbing radiation. The general solution to the local charge conservation Eq.(1) involves the dipole moment per unit length Q(z,t) defined to obey

$$I(z,t) = \frac{\partial Q(z,t)}{\partial t}$$
 and $\lambda(z,t) = -\frac{\partial Q(z,t)}{\partial z}$. (2)

Thus, the electrical currents in one plus one dimensional field theories can be described by a single scalar Boson field Q(z,t) having physical dimension of charge regardless of the fermion field dynamics that may be at the root of the physical motions.

A. Cable Photons in DNA and RNA Chains

Short ranged heavy massive Boson exchange can lead in the vacuum to a point-like Fermion interaction between currents. Boson masses in biological matter are here considered massive if $M_{(heavy boson)}c^2/e \gg \text{millivolt}$. The semiconducting electrons in electrodynamic coherent water[24] domains set the voltage scale of millivolts for the electronic semiconducting energy gaps in biology. For quantum field theories in one spatial dimension, the photons can travel along the molecules as **E** waves or TM cable modes or as **B** waves or TE cable modes. TE and TM mdes along one dimensional cables are massive and exchange of such photons in one spatial dimension lead the Fermi electronic point like or at least short ranged interaction. The vacuum interaction depends on the squre of the current $J^{\mu}J_{\mu} = I^2 - c^2\lambda^2$.

Since the long DNA or RNA chains reside in solution there is a capacitance per unit chain length ε and an inductance per unit chain length μ , the condensed matter Fermi current-current interaction is a simple TEM massless photon. In Gaussian electromagnetic units, there is a zero mass TEM cable mode Lagrangian as grown out of the biological matter point-like Fermi interaction in one spatial dimension

$$L_{TEM} = \frac{1}{2} \int_{\mathcal{L}} \left[\frac{\mu}{c^2} I^2 - \frac{1}{\varepsilon} \lambda^2 \right] dz,$$

$$L_{TEM} = \frac{1}{2} \int_{\mathcal{L}} \left[\frac{\mu}{c^2} \left(\frac{\partial Q}{\partial t} \right)^2 - \frac{1}{\varepsilon} \left(\frac{\partial Q}{\partial z} \right)^2 \right] dz,$$
$$v = \frac{c}{\sqrt{\mu\varepsilon}} \quad \text{wherein} \quad v = \text{ TEM photon velocity.} \quad (3)$$

The quantum electrodynamic zero mass photon quantization from the Lagrangian Eq.(3) is canonical and describes the Goldstone boson for the ordered Tomonaga-Luttinger liquid of electrons.

B. Polymer Chain Thermodynamics

In Sec.II the statistical thermodynamics of a long polymer molecule having energy \mathcal{U} , entropy \mathcal{S} , length \mathcal{L} , dipole moment \mathcal{P} and chemical composition particle numbers $\mathcal{N}_1, \dots, \mathcal{N}_f$ will be discussed in terms of the complete extensive scaling thermodynamic function

$$\mathcal{U} = \mathcal{U}(\mathcal{S}, \mathcal{L}, \mathcal{P}, \mathcal{N}_1, \cdots, \mathcal{N}_f),$$

$$\lambda \mathcal{U} = \mathcal{U}(\lambda \mathcal{S}, \lambda \mathcal{L}, \lambda \mathcal{P}, \lambda \mathcal{N}_1, \cdots, \lambda \mathcal{N}_f),$$

$$d\mathcal{U} = Td\mathcal{S} + \tau d\mathcal{L} + Ed\mathcal{P} + \sum_{a=1}^f \mu_a d\mathcal{N}_a,$$

$$\mathcal{U} = T\mathcal{S} + \tau \mathcal{L} + E\mathcal{P} + \sum_{a=1}^f \mu_a \mathcal{N}_a,$$
(4)

wherein T, τ, E and μ_1, \cdots, μ_f represent respectively the temperature, long molecule tension (negative compression), electric field tangent to the molecule axis and chemical potentials. In terms of *intensive quantities per unit length*

$$\mathcal{U} = u\mathcal{L}, \ \mathcal{S} = s\mathcal{L}, \ \mathcal{P} = Q\mathcal{L}, \ \mathcal{N}_a = \Gamma_a \mathcal{L},$$
$$u = Ts + \tau + EQ + \sum_{a=1}^{f} \mu_a \Gamma_a,$$
$$-d\tau = sdT + QdE + \sum_{a=1}^{f} \Gamma_a d\mu_a ,$$
$$du = Tds + EdQ + \sum_{a=1}^{f} \mu_a d\Gamma_a .$$
(5)

The complete thermodynamic intensive energy per unit length function $u(s, Q, \Gamma_1, \dots, \Gamma_f) \equiv u(s, Q, \Gamma)$ determines the dipole moment per unit length function $Q(s, E, \Gamma)$,

$$Q = -\left(\frac{\partial\tau}{\partial E}\right)_{T,\mu} = -\left(\frac{\partial w}{\partial E}\right)_{s,\Gamma},$$

$$w(s, E, \Gamma) = \inf_{Q} \left(u(s, Q, \Gamma) - EQ\right),$$

$$dw = Tds - QdE + \sum_{a=1}^{f} \mu_a d\Gamma_a.$$
 (6)

The thermodynamic equations of state may be computed from field theoretical models in one spatial z plus one temporal t dimension wherein the spatial coordinate z represents the distance along the axis of the molecule. The current Eqs.(1) and (2) along the molecular axis is completely determined by Q obeying in thermodynamics Eq.(6). Finally, the full Lagrangian for molecular polymer antennae currents read

$$L_{electronic}[Q] = \left(\frac{1}{2\varepsilon}\right) \times \int_{\mathcal{L}} \left[\frac{1}{v^2} \left(\frac{\partial Q}{\partial t}\right)^2 - \left(\frac{\partial Q}{\partial z}\right)^2 - u(s, Q, \mathbf{\Gamma})\right] dz.$$
(7)

The quantum electrodynamic antenna photon quantization from the Lagrangian Eq.(7) is canonical. Eq.(7) holds true in virtue of Eqs.(3) and (5). The above Lagrangian Eq.(7) is a *central result* of this work on DNA and RNA antennae. Ordinary Helmholtz linear electric dipole antennae or loop magnetic dipole antennae are designed employing the physics of linear electromagnetic equations in matter as in the Lagrangian Eq.(3). Natures biological antennae design has been more inventive than was Helmholtz employing nonlinear effects yielding electronic currents for emitting and absorbing photons described by soliton transport. Previously this approach has proved successful in describing polyacetylene and magnetic dipole rings of $(CH)_n$ of the benzene ring (n=6) type.

Finally, additional dissipation processes increasing entropy s in the antennae will give rise to finite lifetime effects for the non-linear collective photon solitons. However these lifetimes become limited to large times by the semiconductor soliton topological stability which amount to identifying soliton fundamental homotopy group kinks as physical electronic charges. Some discussion of photon and phonon absorption is given in Sec.IV.

C. Field Theoretical Models

The simplest example of the field theoretical models applied to a long organic polymer molecule involved trans-polyacetylene whose chain of n links has the chemical formula $(CH)_n$ is discussed in Sec.III and pictured in FIG.1.

The fermion electronic model in one spatial dimension involves the massive Thirring model with a Dirac spinor band kinetic energy plus the Fermi point-wise currentcurrent electron interaction. This point-like Fermi interaction can be renormalized only in a one spatial dimension field theory. Such a Fermion model can also be "bosonized" as noted by Tomonaga[16], Luttinger[17] and Mattis and Lieb[18]. A relativistic view of the renormalized massive Thirring model in one spatial dimension was discussed in great mathematical detail by Coleman[19] who proved the "bosonized" equivalence to the sine-Gordon field theory in one spatial dimension. The connection between the soliton in the quantum field theoretical sine-Gordon model and electronic





FIG. 1: Shown is the molecular structure of a polyacetylene chain $(CH)_n$ of n links. Each carbon atom bonds to a neigboring carbon atom alternating between one and two bonds as in $\cdots - C = C - C = C - C = C - \cdots$. The fourth Carbon bond is attached to a Hydrogen atom. A chain of six links completed as a hexagon represents $C_6H_6 = (CH)_6$, i.e. a benzene ring. A chain completed into a ring or loop acts as a molecular magnetic dipole antenna. Such would also be true of a polymer DNA loop in bacteria or and RNA loop in a virus.

charge transport in polyacetylene polymer chains was discussed in the work on the SSH model[20, 21] (Su, Schrieffer, Heeger). The nature of the soliton Fermion number was explored by Jackiw and Rebbi[22]. In our work the soliton has the charge of one electronic charge as demanded by the connection between local charge conservation and gauge invariance. The soliton structure has been reported observed[23]. The Coleman sine-Gorden equivalence is discussed in Sec.III

D. The Mechanics of Damped Slinky Modes

The two helix DNA model and the single helix RNA model mechanically act similarly to a quantum mechanical molecular toy *helical slinky*. The known mechanical modes of motion of such a slinky is usually called *worm-like* in conventional studies[30] of long polymer chains. The statistical mechanics[27] of the slinky or wormlike motions wherein the long helical biological molecules clump into balls of string or are knitted and folded into sheets of polymer protein material is well studied. These have long been applied to describe biological compaction essential for the central biological mantra of how DNA and RNA produce proteins. These compaction modes are discussed in Sec.??.

The differential geometry of the path of a long spatial winding polymer chain is described by giving the points on a polymer path [28] as a function of arclength s,

$$\mathbf{r} = \mathbf{r}(s)$$
 wherein $ds^2 = d\mathbf{r} \cdot d\mathbf{r}$. (8)

A triad of unit vectors, one tangent \mathbf{t} and two normal \mathbf{n} and $\mathbf{b} = \mathbf{t} \times \mathbf{n}$, create a moving reference frame triad of unit vectors $(\mathbf{t}, \mathbf{n}, \mathbf{b})$ along the curved molecular path. The rotation of the unit orthonormal vector triad obeys

FIG. 2: Shown is the helix of radius R and pitch h generated by constant curvature and constant torsion as in Eq.(10) below. R is the radius of the helical cylinder and for every 2π rotation around the cylinder axis the curve rises a height h.

the equations of Frenet and Serret

$$\frac{d}{ds} \begin{pmatrix} \mathbf{t} \\ \mathbf{n} \\ \mathbf{b} \end{pmatrix} = \begin{pmatrix} 0 & \kappa & 0 \\ -\kappa & 0 & \tau \\ 0 & -\tau & 0 \end{pmatrix} \begin{pmatrix} \mathbf{t} \\ \mathbf{n} \\ \mathbf{b} \end{pmatrix}, \qquad (9)$$

wherein κ is the *curvature* of the molecule and τ is the *torsion* of the molecule. In order to understand the meaning of curvature and torsion, conseder the case wherein the curvature and torsion are uniform along the curve, i.e.

$$\kappa = \frac{1}{R}, \quad \tau = \frac{2\pi}{h} \tag{10}$$

for the case that R = const. and h = const. generates a helix as shown in FIG.2

In the Kratky-Porod model, also known as the wormlike chain model[30–32], the DNA and/or RNA the polymer helices wiggle about like worms in the fluid solute environment. The energy of a worm-like chain or more briefly a deformed slinky-wormlike polymer is described by the energy

$$\mathcal{U}_{\text{deformation}} = \tilde{\tau}\mathcal{L} + \frac{\mathcal{Y}}{2} \int_{\mathcal{L}} \left[\xi_1^4 \kappa(s)^2 + \xi_2^4 (\tau(s) - \tau_0)^2 \right] ds, \tag{11}$$

wherein the tension $\tilde{\tau} > 0$ or compression $\tilde{\tau} < 0$ in the first term on the right hand side of Eq.(11) here has an overhang $\tilde{\tau}$ only to distinguish it from torsion τ . This first term treats the wormlike slinky motions as in string theory with the long chain molecular "string" embedded in the physical three spatial dimensions. The second two terms on the right hand side of Eq.(11) give rise to rigidity in transverse mechanical vibrations and torsional (or angular) mechanical vibrations that affect the mechanical vibrations giving rigidity to the polymer chain. The Young's modulus is denoted by \mathcal{Y} and the Poisson ratio is denote by σ . Here we are applying classical elasticity theory[29]. In *bulk solids*, there is one longitudinal sound wave velocity and two modes of transverse sound velocity as given by

$$v_{\text{long}} = \sqrt{\frac{\mathcal{Y}(1-\sigma)}{\rho(1-\sigma)(1-2\sigma)}}$$
 Bulk Longitudinal,
 $v_{\text{trans}} = \sqrt{\frac{\mathcal{Y}}{2\rho(1+\sigma)}}$ Bulk Transverse, (12)

Finally, the persistance lengths of the polymer rigidity will be denoted by ξ_j .

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Helical DNA and RNA Curvature and Torsion in Wormlike Slinky Modes Refer to the Bending Curve Center Axis of the Molecule from Transverse Motions

FIG. 3: Shown above schematically are two longitudinal modes and two transverse modes. The longitudinal modes are determined if the "center line" of the helices is straight. (a) The two longitudinal degrees of freedom can be taken as R(z,t), the local radius of the straight coil and h(z,t) the local pitch of the straight coil. The z-axis is a straight line. The physical picture of the two longitudinal modes is linear compression and local rotational displacement both with an associated Poisson ratio. (b) The two transverse modes have curved central lines with arc length ds and distortion energy Eq.(11).

There are four modes of mechanical waves on helical polymer molecules in a worm like chain as shown in FIG.3. Their exists four kinds of mechanical waves of interest: (i) There are two longitudinal modes with a straight line z-axis as the center of of the coils. There is compressional sound in a cylinder and rotational sound due to torsion. (ii) There are two transverse degrees of freedom for the *now curved central axis* of the coil as in Eq.(11).

Associated with bulk polymer mass density ρ is a longitudinal persistance length ξ_l defined thermodynamically by

$$\rho_1 \equiv \left(\sum_{a=1}^f m_a \Gamma_a\right) = \rho \xi_l^2 \tag{13}$$

wherein m_a is the mass of chemical species a on the polymer chain and ρ_1 is the mass per unit length of the chain.

For small oscillations in the elastic strain, the first longitudinal compressional mode in a thin straight wormslinky has a sound velocity spectrum

$$\omega = v_l k$$
 compressional $v_l = \sqrt{\frac{\mathcal{Y}}{\rho}}$. (14)

The second straight central axis mode is torsional with spectrum

$$\omega = D_l k^2 \quad \text{torsional} \quad D_l = v_l \xi_l. \tag{15}$$

Typically, longitudinal compressional mode velocities $v_l \sim 2 \times 10^5$ cm/sec, while persistence lengths are approximately the coherent domain sizes in water[24, 25], $\xi \sim 5 \times 10^{-6}$ cm. Thus $D_l \sim 1 \text{ cm}^2/\text{sec}$. Note the electron quantum of circulation $D_{\rm el} = (\hbar/m) \approx 1.16 \text{ cm}^2/\text{sec}$ contributing to the free electron spectrum $E = \hbar^2 k^2/2m$. The agreement $D_{\rm el} \sim D_l$ is not fortuitous. Finally, the transverse bending modes for the wormlike-slinky have the spectrum

$$\omega = D_t k^2 \quad \text{transverse} \quad D_l = v_t \xi_t. \tag{16}$$

which is degenerate if the staight line axis does not sense an asymptry in the rotational moments of inertia. Here ξ_t is the transverse persistance length. These frequencies quadratic in the wave number k are comparable to free electron Bohr transition frequencies, $\hbar\omega_{fi} = E_f - E_i$, wherein $E = \hbar^2 k^2/2m$, obey

$$\omega_{fi} = \frac{1}{2} D_{\rm el} \left[(k_f + k_i)(k_f - k_i) \right] \quad \text{with} \quad D_{\rm el} = \frac{\hbar}{m}. \quad (17)$$

The similar orders of magnitude $D_l \sim D_{\rm el}$ are not fortuitous. Young's modulus describes the internal pressureenergy as determined by the electron Pauli exclusion principle required for stable matter when Coulomb forces are of microscopic importance.

E. Electric and Magnetic Dipole Antennae

In Sec.V the electric dipole antenna that constitutes a linear axis DNA or ENA chain polymer molecule subject to an electric field is described by the massive Thirring sine Gordon Lagrangian in a driving electric E field

$$L_{electronic}[Q] = \left(\frac{1}{2\varepsilon}\right) \times \int_{\mathcal{L}} \left[\frac{1}{v^2} \left(\frac{\partial Q}{\partial t}\right)^2 - \left(\frac{\partial Q}{\partial z}\right)^2\right] dz - \int_{\mathcal{L}} \left[\hbar \varpi \left(1 - \cos\left(2\pi \frac{Q}{e}\right)\right) - EQ\right] dz, \qquad (18)$$

corresponding to the equation of motion

$$\left[\frac{\varepsilon}{v^2} \left(\frac{\partial}{\partial t}\right)^2 - \left(\frac{\partial}{\partial z}\right)^2\right] Q + \left(\frac{2\pi\hbar\omega}{e}\right) \sin\left(2\pi\frac{Q}{e}\right) = E.$$
 (19)

If the driving electric field depends only on time

$$E(t) = -\frac{1}{c}\dot{A}(t)$$
 and $\mathcal{P} = \mathcal{L}Q(t)$, (20)

then only the total electric dipole moment \mathcal{P} comes into the equations of motion. In the electric dipole limit we thereby have the ordinary differential equation corresponding to a voltage V(t) driven pendulum with a current output $I(t) = \dot{Q}(t)$,

$$\frac{L}{c^2}\ddot{Q}(t) + V_c \sin\left(2\pi \frac{Q(t)}{e}\right) = V(t).$$
(21)

wherein the antenna inductance $L = \mu \mathcal{L}$, the driving voltage $V(t) = E(t)\mathcal{L}$ and the critical voltage is defined $V_c = (2\pi\hbar\omega/e)\mathcal{L}$.

If the electron oscillations on the straight axis of the have a finite dissipation increasing the molecular entropy by heating, then phenomenologically a resistance R may be added to the electric dipole antenna model according to $I(t) = \dot{Q}(t)$,

$$\frac{L}{c^2}\ddot{Q}(t) + R\dot{Q}(t) + V_c \sin\left(2\pi \frac{Q(t)}{e}\right) = V(t).$$
(22)

For the moment neglecting resistance, the driven electric dipole antenna as a quantum electrodynamic circuit described by the ordinary Lagrangian

$$\Lambda(\dot{Q},Q) = \frac{L}{c^2}\dot{Q}^2 + \frac{\mathcal{L}\dot{AQ}}{c}$$
$$\left(\frac{eV_c}{2\pi}\right)\left[1 - \cos\left(2\pi\frac{Q}{e}\right)\right].$$
(23)

in virtue of Eq.(20).

The Hamiltonian operator corresponding to the Lagrangian Eq.(20) is canonical

$$\mathcal{H}(\Phi_{\text{ext}}) = \frac{1}{2L} \left(-i\hbar c \frac{\partial}{\partial Q} - \Phi_{\text{ext}} \right)^2 + \left(\frac{eV_c}{2\pi} \right) \left[1 - \cos\left(2\pi \frac{Q}{e}\right) \right].$$
(24)

Here the driving vector potential is $A = \Phi_{\text{ext}}/\mathcal{L}$. By wrapping up the linear electric dipole antenna into a loop one obtains the magnetic dipole antennae with a total magnetic moment given by a current area product.

In detail, the external magnetic flux through the loop is given by

$$\Phi_{\text{ext}} = \oint \mathbf{A} \cdot d\mathbf{r} = \int_{\mathcal{L}} A ds. \qquad (25)$$

The Schrödinger equation for the loop is given by

$$i\hbar \frac{\partial \psi(Q,t)}{\partial t} = \mathcal{H}(\Phi_{\text{ext}})\psi(Q,t)$$
 (26)

wherein the Hamiltonian is identical to the electric dipole antenna Hamiltonian Eq.(24); However, the *magnetic*

dipole antennae boundary condition defining the geometrical meaning of "loop" is the magnetic dipole boundary periodic condition

$$\psi(Q+e,t) = \psi(Q,t)$$
 magnetic dipole loop. (27)

In particular, as a consequence of Eq.(27) the energy eigenvalues are periodic in external magnetic flux, i.e.

$$\mathcal{H}(\Phi_{\text{ext}})\psi_n(Q) = E_n(\Phi_{\text{ext}})\psi_n(Q),$$

$$\psi_n(Q+e) = \psi_n(Q),$$

$$E_n(\Phi_{\text{ext}} + \Phi_0) = E_n(\Phi_{\text{ext}}),$$
(28)

wherein the flux quantum is given by

$$\Phi_0 = \frac{2\pi\hbar c}{e} \ . \tag{29}$$

According to present international agreements on SI units wherein the electromagnetic charge conversion is exactly 1 emu $\equiv 10$ Coulomb and 1 Tesla $\equiv 10^4$ Gauss we have the exact three unit definitions

$$c \equiv 2.99792458 \times 10^{10} \frac{\text{cm}}{\text{sec}} ,$$

$$2\pi\hbar \equiv 6.62607015 \times 10^{-27} \text{ erg sec},$$

$$\frac{e}{c} \equiv 1.602176634 \times 10^{-20} \text{ emu.}$$
(30)

The flux quantum is then

$$\Phi_0 \approx 4.135667697 \times 10^{-7} \text{ Gauss cm}^2.$$
 (31)

Many distinctive properties of DNA or RNA molecular antennae follow from the periodicities of the circulating currents

$$I_n(\Phi_{\text{ext}}) = I_n(\Phi_{\text{ext}} + \Phi_0). \tag{32}$$

Eq.(32) follows from

$$I_n(\Phi_{\text{ext}}) = -c \frac{dE_n(\Phi_{\text{ext}})}{d\Phi_{\text{ext}}}$$
(33)

in virtue of Eq.(29). The magnetic flux periodicity of circulating currents in molecular dipole antennae arises out of electrodynamic gauge invariance and the Bohm Aharoniv effect and is likely to surpass the accuracy of particular model Hamiltonians such as ours playing a strong role wireless transmission of information between DNA and/or RNA molecules.

II. STATISTICAL THERMODYNAMICS

Of interest here are electrical and mechanical vibrations that quantize into photons and phonons in the usual manner. Photon-phonon conversions can and do take the form of piezoelectricity that go into the design of ultrasound emitters and absorbers[33]. A simple understanding of piezoelectricity can be obtained by the general principles of statistical thermodynamics. The role of this reasoning is of use for understanding biological piezoelectricity as it occurs in long stands of DNA and RNA due to the lack of chiral (handed) symmetry in helical molecules.

A. Quartz Crystal Ultrasound

To get ultrasound generators from a quartz crystal it is sufficient to cleave the crystal so that a given crystal plane appears parallel on two sides of the quartz sample. Then deposit two metallic films, one on each of the opposite flat sides of the quartz sample forming a circuit capacitor depositing equal and opposite charges on the two metallic plates. The thermodynamic equations of state of the capacitor follow from the fundamental law

$$d\mathcal{U} = Td\mathcal{S} + \mathcal{V}dQ + \mathcal{F}dX, \tag{34}$$

wherein S, Q and X represent, respectively, the capacitor entropy, charge and quartz crystal plane displacement and T, \mathcal{V} , and \mathcal{F} represent, respectively, the capacitor temperature, voltage and force component parallel to the plane displacement that the metallic film exerts on the quartz crystal. Alternatively, one may employ the capacitor enthalpy

$$\mathcal{W}(\mathcal{S}, \mathcal{V}, X) = \min_{Q} \left[\mathcal{U}(\mathcal{S}, Q, X) - \mathcal{V}Q \right].$$

$$d\mathcal{W} = Td\mathcal{S} - Qd\mathcal{V} + \mathcal{F}dX. \tag{35}$$

The capacitances at constant displacement X and at constant force \mathcal{F} are defined respectively as

$$C_X = \left(\frac{\partial Q}{\partial \mathcal{V}}\right)_{\mathcal{S},\mathcal{X}} \text{ and } C_\mathcal{F} = \left(\frac{\partial Q}{\partial \mathcal{V}}\right)_{\mathcal{S},\mathcal{F}}.$$
 (36)

Employing thermodynamic derivative identities

$$\begin{pmatrix} \frac{\partial Q}{\partial \mathcal{V}} \end{pmatrix}_{\mathcal{S},\mathcal{F}} = \left(\frac{\partial Q}{\partial \mathcal{V}} \right)_{\mathcal{S},\mathcal{X}} + \left(\frac{\partial Q}{\partial X} \right)_{\mathcal{S},\mathcal{V}} \left(\frac{\partial X}{\partial \mathcal{V}} \right)_{\mathcal{S},\mathcal{F}} ,$$

$$C_{\mathcal{F}} = C_X - \left(\frac{\partial Q}{\partial X} \right)_{\mathcal{S},\mathcal{V}} \left(\frac{\partial X}{\partial \mathcal{F}} \right)_{\mathcal{S},\mathcal{V}} \left(\frac{\partial \mathcal{F}}{\partial \mathcal{V}} \right)_{\mathcal{S},\mathcal{X}} ,$$

$$C_{\mathcal{F}} = C_X + \frac{\Lambda_{\mathcal{S}}^2}{K_{\mathcal{S}}} , (37)$$

wherein the adiabatic piezoelectric coefficient is defined by a Maxwell relation for the enthalpy Eq.(35)

$$\Lambda_{\mathcal{S}} = \left(\frac{\partial Q}{\partial X}\right)_{\mathcal{S},\mathcal{V}} = -\left(\frac{\partial \mathcal{F}}{\partial \mathcal{V}}\right)_{\mathcal{S},\mathcal{X}} .$$
(38)

The thermodynamic adiabatic static Hook's law spring constant for the vibrational quartz mode is defined

$$\mathcal{K}_{\mathcal{S}} = \left(\frac{\partial \mathcal{F}}{\partial X}\right)_{\mathcal{S},\mathcal{V}} \,. \tag{39}$$

The central result of this section is that a measured capacitance of the quartz filled capacitor is a circuit parallel connection between two capacitors: (i) a capacitance C_X wherein the position of the vibrational mode is clamped and (ii) an elastic capacitance

$$C_{\mathcal{F}} = C_X + C_{\text{elastic}} ,$$

$$C_{\text{elastic}} = \frac{\Lambda_{\mathcal{S}}^2}{\mathcal{K}_{\mathcal{S}}} , \qquad (40)$$

adding capacitance for the parallel circuit connection. Using a damped harmonic oscillator model for the quartz vibrational phonon mode, yields a complex frequency dependent elastic electrical engineering capacitance

$$\mathcal{M}\delta\ddot{X}(t) + \mathcal{R}\delta\dot{X}(t) + \mathcal{K}_{\mathcal{S}}\delta X(t) = \delta\mathcal{F}(t),$$

$$C_{\text{elastic}}(\omega) = \frac{\Lambda_{\mathcal{S}}^2}{\mathcal{K}_{\mathcal{S}} - i\omega\mathcal{R} - \omega^2\mathcal{M}},$$

$$C_{\text{elastic}}(\omega) = \frac{\omega_0^2 C_{\text{elastic}}}{\omega_0^2 - i\Gamma\omega - \omega^2}.$$
(41)

wherein \mathcal{M} is the mass of the vibrational mode and \mathcal{R} is the mechanical acoustic impedance of the vibrational mode. The frequency ω_0 of the quartz phonon mode is and the inverse phonon lifetime $\tau_{\text{phonon}}^{-1} = \Gamma$ is determined in mechanical engineering terms as

$$\omega_0 = \sqrt{\frac{\mathcal{K}_S}{\mathcal{M}}} \quad \text{and} \quad \Gamma = \frac{\mathcal{R}}{\mathcal{M}} .$$
 (42)

The frequency dependent circuit admittance of the fix displacement capacitance connected in parallel with the elastic mode capacitance is

$$Y(\omega) = -i\omega [C_X + C_{\text{elastic}}(\omega)],$$

$$Y(\omega) = -i\omega \left[C_X + \frac{\omega_0^2 C_{\text{elastic}}}{\omega_0^2 - i\Gamma\omega - \omega^2} \right],$$

$$\Re eY(\omega) = \omega_0^2 \Gamma \left[\frac{\omega}{(\omega^2 - \omega_0^2)^2 + \omega^2 \Gamma^2} \right] C_{\text{elastic}}.$$
 (43)

If a voltage source \mathcal{V}_{ω} at frequency ω is placed across the quartz crystal filled capacitor, then the dissipated power $P(\omega) = |\mathcal{V}_{\omega}|^2 \Re eY(\omega)$ is mostly due to to a sharp phonon peak as described by Eq.(43). The dissipative power mostly goes into phonon radiation from the quartz mechanical oscillator that becomes a source of ultrasound at a sharp frequency. Let us now apply similar thermodynamic arguments to long DNA and RNA molecules as we have above reviewed for standard ultrasonic crystal sources.

B. DNA and RNA Piezoelectricity

For describing the piezoelectric effect in DNA and RNA molecules, start from the dipole moment enthalpy

$$\tilde{\mathcal{W}} = \min_{Q} \left[\mathcal{U}(\mathcal{S}, \mathcal{L}, \mathcal{P}, \mathcal{N}_{1}, \cdots, \mathcal{N}_{f}), -E\mathcal{P} \right],$$
$$\tilde{\mathcal{W}} = \tilde{\mathcal{W}}(\mathcal{S}, \mathcal{L}, E, \mathcal{N}_{1}, \cdots, \mathcal{N}_{f}),$$
$$d\tilde{\mathcal{W}} = Td\mathcal{S} + \tau d\mathcal{L} - \mathcal{P}dE + \sum_{a=1}^{f} \mu_{a} d\mathcal{N}_{a},$$
$$\tilde{\mathcal{W}} = T\mathcal{S} + \tau \mathcal{L} + \sum_{a=1}^{f} \mu_{a} \mathcal{N}_{a}.$$
(44)

With $\mathcal{N} = \sum_{a=1}^{f} \mathcal{N}_a$ intensive per constituent particle are defined as

$$x_{a} = \frac{\mathcal{N}_{a}}{\mathcal{N}} , \quad \sum_{a=1}^{J} x_{a} = 1,$$
$$\tilde{w} = \frac{\mathcal{\tilde{W}}}{\mathcal{N}} , \quad \tilde{s} = \frac{\mathcal{\tilde{S}}}{\mathcal{N}} , \quad l = \frac{\mathcal{\tilde{L}}}{\mathcal{N}} , \quad \tilde{p} = \frac{\mathcal{\tilde{P}}}{\mathcal{N}} = lQ,$$
$$\tilde{w} = T\tilde{s} + \tau l + \sum_{a=1}^{f} \mu_{a} x_{a}, \quad (45)$$

in virtue of which

$$d\tilde{w} = Td\tilde{s} + \tau dl - \tilde{p}dE + \sum_{a=1}^{f} \mu_a dx_a.$$
 (46)

1. Static Piezoelectricity

The static adiabatic *piezoelectric coefficient* of a long polymer molecules is defined as

$$\lambda_{\tilde{s}} = \left(\frac{\partial \tau}{\partial E}\right)_{\tilde{s},l,\mathbf{x}} = -\left(\frac{\partial \tilde{p}}{\partial l}\right)_{\tilde{s},E,\mathbf{x}},\tag{47}$$

wherein a Maxwell relation implicit in Eq.(46) has been employed. Two molecular polarizability coefficients may be defined (i) at constant molecular tension τ and (ii) at constant molecular length l; They are, respectively,

$$\alpha_{\tau} = \left(\frac{\partial \tilde{p}}{\partial E}\right)_{\tilde{s},\tau,\mathbf{x}} \quad \text{and} \quad \alpha_{l} = \left(\frac{\partial \tilde{p}}{\partial E}\right)_{\tilde{s},l,\mathbf{x}}.$$
(48)

The difference is by partial differentials is evidently

$$\alpha_{\tau} = \alpha_{l} + \left(\frac{\partial \tilde{p}}{\partial l}\right)_{\tilde{s},l,\mathbf{x}} \left(\frac{\partial l}{\partial E}\right)_{\tilde{s},\tau,\mathbf{x}},$$

$$\alpha_{\tau} = \alpha_{l} - \left(\frac{\partial \tilde{p}}{\partial l}\right)_{\tilde{s},l,\mathbf{x}} \left(\frac{\partial l}{\partial \tau}\right)_{\tilde{s},E,\mathbf{x}} \left(\frac{\partial \tau}{\partial E}\right)_{\tilde{s},l,\mathbf{x}},$$

$$\alpha_{\tau} = \alpha_{l} + \frac{\lambda_{\tilde{s}}^{2}}{\kappa_{\tilde{s}}}, \quad (49)$$

wherein the hook law adiabatic spring constant $\kappa_{\tilde{s}}$ per molecule for a long molecule is defined

$$\kappa_{\tilde{s}} = \left(\frac{\partial \tau}{\partial l}\right)_{\tilde{s}, E, \mathbf{x}}.$$
(50)

The fundamental theorem of thermodynamics for how piezoelectricity in long DNA or RNA molecular polarizability is thereby

$$\alpha_{\tau} = \alpha_l + \alpha_{\text{elastic}} \quad \text{wherein} \quad \alpha_{\text{elastic}} = \frac{\lambda_{\tilde{s}}^2}{\kappa_{\tilde{s}}} , \qquad (51)$$

plays the same role in long polymer piezoelectric physics that Eq.(40) plays for quartz piezoelectricity. Classical thermal fluctuations in the molecular tension obey

$$\overline{\Delta\tau^2} = \frac{k_B T}{\mathcal{N}} \left(\frac{\partial\tau}{\partial l}\right)_{\tilde{s}, E, \mathbf{x}} = k_B T \left(\frac{\kappa_{\tilde{s}}}{\mathcal{N}}\right),$$
$$\overline{\Delta\tau^2} = k_B T \left(\frac{\partial\tau}{\partial\mathcal{L}}\right)_{\mathcal{S}, E, \mathcal{N}_1, \cdots, \mathcal{N}_f} = k_B T \mathcal{K}_{\mathcal{S}} \qquad (52)$$

wherein the overall adiabatic spring constant of the molecule is inversely proportional to the number of constituent molecules $\mathcal{K}_{\mathcal{S}} = \kappa_{\tilde{s}}/\mathcal{N}$ On the other hand the mode mass for a homogeneous slinky-worm oscillation is extensive $\mathcal{M} = \mathcal{N}m_0$ wherein m_0 is of the order of the mean molecular mass. This means that the frequency of the homogeneous compression mode is given by

$$\Omega = \sqrt{\frac{\mathcal{K}_{\mathcal{S}}}{\mathcal{M}}} = \frac{\omega_0}{\mathcal{N}} \to 0 \quad \text{as} \quad \mathcal{N} \to \infty.$$
 (53)

Given the virtually zero frequency of the homogeneous longitudinal dissipation, the mode is completely dissipative.

2. Vibrational Dissipation

For mechanical vibrations coupling into antennae currents via piezoelectric coefficients, an engineering approach may generalize the static quartz oscillator coupling Eq.(40) that in dynamic situations reads as Eq.(41). The close analogy is that the dynamic engineering dynamical version of Eq.(51) is given by

$$\alpha_{\tau} = \alpha_l + \alpha_{\text{elastic}} \sum_j \left[\frac{f_j \omega_j^2}{\omega_j^2 - i\omega\Gamma_j - \omega^2} \right], \quad (54)$$

wherein the sum is over mechanical modes described by damped harmonic oscillators with oscillator strengths $f_j > 0$ that sum to unity, i.e. $\sum_j f_j = 1$. In Eq.(54), ω_j represents the mechanical resonance frequency of the phonon and Γ_j represents the transition rate per unit time per unit time that the phonon is absorbed as heat energy into other degrees of freedom. One may introduce a damping force correlation time τ_j of the random force from these other degrees of freedom that damp the mechanical oscillation according to Fermi's golden rule

$$\Gamma_{j} = \frac{2\pi}{\hbar} |\hbar\omega_{j}|^{2} \left(\frac{\tau_{j}}{2\pi\hbar}\right),$$

$$\Gamma_{j} = \omega_{j}^{2} \tau_{j} \quad \Rightarrow \quad \frac{\Gamma_{j}}{\omega_{j}} = \omega_{j} \tau_{j} .$$
(55)

Eq.(54) describes how the mechanical modes enter into the electrodynamic properties of DNA and RNA antennae only if the modes are lightly damped $\omega_j \tau_j \ll 1$. If the phonon modes are very highly damped by viscous forces then Eq.(54) is nor adequate. The physical principles follow below. Consider the original Stokes problem i.e. damping from a solid surface contact with a viscous fluid. Consider the formally infinite surface problem wherein the solid is in the half space z < 0 and the viscous fluid is in the half space z > 0 and the oscillation of the solid surface is in the x-direction. If $v_x(z,t)$ is the only non-zero fluid velocity component in the fluid mechanical NavierStokes equations, then the velocity V(t) and the force per unit area that the fluid exerts on the solid surface F(t) obey, respectively,

$$V(t) = \lim_{z \to 0^+} v_x(z, t) \text{ and}$$
$$F(t) = -\eta \lim_{z \to 0^+} \left(\frac{\partial v_x(z, t)}{\partial z}\right).$$
(56)

The velocity diffusion equation with viscosity η and mass density ρ is here written within the fluid as

$$\rho \frac{\partial v_x(z,t)}{\partial t} = \eta \frac{\partial^2 v_x(z,t)}{\partial z^2}.$$
(57)

In virtue of fractional derivative identities [34] one may take the "operator square root" of Eq.(57)

$$\sqrt{\rho \frac{\partial}{\partial t}} v_x(z,t) = \sqrt{\eta} \frac{\partial v_x(z,t)}{\partial z}$$
(58)

yielding the force per unit area as a functional of the slinding surface velocity

$$F(t) = -\sqrt{\rho\eta} \left[\sqrt{\frac{\partial}{\partial t}} \right] V(t),$$
$$F(t) = -\sqrt{\rho\eta} \left[\sqrt{\frac{1}{\pi}} \int_0^\infty \frac{ds}{\sqrt{s}} e^{-s\partial/\partial t} \right] V(t),$$
$$\frac{F(t)}{\rho} = -\sqrt{\frac{\nu}{\pi}} \int_0^\infty \frac{ds}{\sqrt{s}} V(t-s) \text{ wherein } \eta = \rho\nu, (59)$$

in virtue of Eq.(56) and the evaluation of the integral $\sqrt{\pi a} = \int_0^\infty e^{-as} ds / \sqrt{s}$.

The drag force per unit surface area F(t) is a nonlocal in time functional of the surface velocity V(t) for an incompressible fluid with kinematic viscosity ν . The kinematic viscosity represents the diffusion of liquid vorticity at a rate in water of

$$\nu \approx 10^{-2} \frac{\text{cm}^2}{\text{sec}} = 10^4 \text{ Hz} \times (10 \text{ micron})^2 \text{ (water). (60)}$$

For distance ~ 10 micron say within a biological cells for many types of cells, the mechanical modes exhibit strongly viscous damping for frequencies $\omega < 10$ KHz. The strong damping leads to fractional exponent in the imaginary part of the dielectric response ~ $\omega^{-1/2}$ as $\omega \to 0$. Confinement geometries more generally lead to dynamic fractional exponents ~ ω^{-z} as $\omega \to 0$ even in pure water wherein the extremely high dielectric response as $\omega \to 0$ has a domain size scale of ordered water[24, 25].

III. MASSIVE QED THIRRING MODEL

The mass term employing Dirac spinors yields the invarient energy density

$$u_{\rm mass} = -m_{\rm electron} c^2 \bar{\psi} \psi \tag{61}$$

wherein ψ is the electron wave function. If the Dirac matrices are written in the representation in which the left and right chiral matrix is diagonal, then the notion of mass comes from matrix elements that connect right to left chirality. In one spatial dimension, fix the spin and consider the two element electron wave function for left and right handed electrons,

$$\psi = \begin{pmatrix} \psi_R \\ \psi_L \end{pmatrix} \quad \text{wherein} \quad \bar{\psi}\psi = \psi_R^*\psi_L + \psi_L^*\psi_R. \tag{62}$$

If the left and right amplitudes have phases,

$$\psi_{R,L} = |\psi_{R,L}| e^{i\vartheta_{L,R}} \equiv \sqrt{\frac{n_{\text{pair}}}{2}} e^{i\vartheta_{L,R}},$$

$$\psi_{R}^{*}\psi_{L} + \psi_{L}^{*}\psi_{R} = n_{\text{pair}}\cos(\vartheta_{R} - \vartheta_{L})$$
(63)

wherein $n_{\text{pair}} = (1/2)|\psi_R\psi_L|$ are the number of bound particle-hole pairs per unit length, then the phase difference implicit in Eq.(62)

$$\vartheta_R - \vartheta_L = 2\pi \frac{Q}{e} , \qquad (64)$$

yields the energy density

$$u_{\rm mass} = -\hbar\varpi\cos\left(2\pi\frac{Q}{e}\right).\tag{65}$$

in virtue of quantum phase interference between the left and right handed chirality states. In Eq.(66), $m_{\text{electron}}c^2n_{\text{pair}} = \hbar \varpi$. A convention adds a constant to this energy to make a model energy density u(Q),

$$u(Q) = \hbar \varpi \left[1 - \cos \left(2\pi \frac{Q}{e} \right) \right], \tag{66}$$

to employ in the Coleman sine Gordon Lagrangian Eq.(18). This completes our derivation of Coleman's result that a massive Thirring Fermion model of electrons in a quasi-linear system is equivalent to a sine Gordon Boson model.

IV. SLINKY DAMPED MECHANICS OF THE LONGITUDINAL SOUND MODE

Here wer consider the viscous damping of a pure longitudinal wave in a slinky helix. The viscous damping is mainly due to the electronic viscosity that is in turn caused by the electrical conductivity. The molecular ultrasonoic phonon ansorption is thereby due to the electronic Landau-Fermi liquid consuctivity in a bulk metal[35] but is here is due to the Tomonoga-Luttinger[16–18] liquid in DNA or RNA long helicalslinky polymer molecules. Thermodynamics as dictated by Sec.IIB is determined by

$$d\tilde{u} = Td\tilde{s} + \tau dl + Ed\tilde{p} + \sum_{a=1}^{f} \mu_a dx_a,$$

$$d\tilde{w} = Td\tilde{s} + \tau dl - \tilde{p}dE + \sum_{a=1}^{f} \mu_a dx_a,$$
 (67)

()

yielding the thermodynamic identity

$$\kappa_{\tilde{s}} = \left(\frac{\partial \tau}{\partial l}\right)_{\tilde{s}, E, \mathbf{x}},$$

$$\kappa_{\tilde{s}} = \left(\frac{\partial \tau}{\partial l}\right)_{\tilde{s}, \tilde{p}, \mathbf{x}} + \left(\frac{\partial \tilde{p}}{\partial l}\right)_{\tilde{s}, E, \mathbf{x}} \left(\frac{\partial \tau}{\partial \tilde{p}}\right)_{\tilde{s}, l, \mathbf{x}},$$

$$\kappa_{\tilde{s}} = \kappa_{\tilde{s}l} + \left(\frac{\partial \tilde{p}}{\partial l}\right)_{\tilde{s}, E, \mathbf{x}} \left(\frac{\partial \tau}{\partial E}\right)_{\tilde{s}, l, \mathbf{x}} \left(\frac{\partial E}{\partial \tilde{p}}\right)_{\tilde{s}, l, \mathbf{x}},$$

$$\kappa_{\tilde{s}} = \kappa_{\tilde{s}l} - \left(\frac{\partial \tau}{\partial E}\right)_{\tilde{s}, l, \mathbf{x}}^{2} \left(\frac{\partial E}{\partial \tilde{p}}\right)_{\tilde{s}, l, \mathbf{x}},$$

$$\kappa_{\tilde{s}} = \kappa_{\tilde{s}l} - \left(\frac{\lambda_{\tilde{s}}^{2}}{\alpha_{l}}\right) \cdot (68)$$

To get the frequency dependent hooks law force constant for a uniform compression or extension in electrical engineering terms, one extends Eq.(68) to the upper half complex frequency plane $\zeta = \omega + i \varpi$ wherein $\varpi > 0$,

$$\kappa(\zeta) = \kappa_{\tilde{s},l} - \left[\frac{\lambda_{\tilde{s}}^2}{\alpha_l(\zeta)}\right].$$
(69)

In terms of the electrical engineering intensive impedance $\mathcal{Z}(\zeta)$ of the polymer DNA or RNA chain,

$$\mathcal{Z}(\zeta) = \frac{i}{\zeta n_{el} \alpha(\zeta)} ,$$

$$\kappa(\zeta) = \kappa_{\tilde{s},l} + i \zeta n_{el} \lambda_{\tilde{s}}^2 \mathcal{Z}(\zeta), \qquad (70)$$

wherein $n_{\rm el}$ is the electron density per unit length of chain. The ultrasonic attenuation of the chin molecule is determined by

$$\Im m\kappa(\omega + i0^+) = \left(n_{\rm el}\lambda_{\tilde{s}}^2\right)\omega \Re e\mathcal{Z}(\omega + i0^+) \tag{71}$$

that constitutes the mathematical expression of the physical fact that the piezoelectric coupling allows one to see in the longitudinal sound attenuation that observable by the electrical antenna impedance $\mathcal{Z}(\omega + i0^+)$.

V. MICROBE COMMUNITY ANTENNAE

Microbial communities in the form of films adsorbed on solid substrates live much longer on insulating surfaces than on conducting metallic substances. For example, a community of COVID-19 viruses live typically for a few days on an insulator surface but only a few hours on a metallic surface. This fact makes metallic material insertions of for example copper into cloth hospital face masks of some utility. Microbial communities of electrogenic bacteria adsorbed on a chemical battery cathode employ an insulating adsorption surface although the battery lead cables are eventually metallic. A working hypothesis is that the community of microbes require for healthy living that DNA and RNA antennae within the community constitute a coherent phased array. The dissipative eddy currents within a metal surface will lesson the coherence of the array of antennae. Since the art of experimental biochemistry is closely entwined with the art of fine cooking, those experienced in baking breads should take note that baking yeast has DNA antennae of comparable size to bacteria. Spectroscopic measurements with a radio frequency spectrum analyzer while living processes are under way would be of interest as would other standard Josephson array measurements long understood for superconducting arrays.

VI. CONCLUSIONS

Electrogenic micro-organisms live within environments wherein they are wired to one another or are wired to environmental surfaces. Electronic currents can flow through these wires into and out of biological cells through the cell walls. Of interest in the work described above was the wireless communication that can be radiated from a distance into and out of biological cells wherein the DNA or the RNA molecules can act as antennae that receive or emit radio frequency electromagnetic signals. Alternative to the chemical information carried in the DNA or RNA letter coding, communication information can be carried from a distance in the form of thermodynamic radiation signal entropy. Due to biological piezoelectricity, the electromagnetic radiation is appreciably coupled into ultrasonic acoustic radiation. Thus electromagnetic as well as acoustical spectroscopy is evidently possible.

The helices or double helices, respectively, within RNA and DNA exhibit chiral symmetry breaking (handedness) as must the electronic energy structure. The electronic structure must also properly require chiral symmetry breaking. The electron as an elementary particle carries two possible spin states \uparrow or \downarrow as well as two chiral states right R or left L. Thus we argued, as discovered by Dirac, the electron requires a four component spinor for its description. These four components are required for describing chiral symmetry breaking even if the electrons have kinetic energies small on the scale of the electron rest mass energy.

DNA and RNA as long polymer molecules are quasione dimensional. This, coupled with the chiral symmetry breaking, suggested that the electronic structure has the structure of a Tomonaga-Luttinger liquid wherein there particle-hole bound states. The bound state of a electron particle-hole pair is a Boson and the Tomonaga-Luttinger liquid is a condensation of these Bosons in a manner closely analogous to the Bose condensation of particle-particle or hole-hole bound states in a superconductor. In a superconductor the phase of the Bose pairing field gives rise to Josephson effects. In the biological Tomonaga-Luttinger electron liquid we employed the phase difference between right and left handed electron components to describe the quantum coherence leading to Josephson effects. In both cases the Josephson effects lead to a quantum pendulum, i.e. a sine Gordon boson field model as first demonstrated by Coleman. The

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physical principle involved is that Josephson effects occur whenever the coherent quantum liquid is forced to flow through weak links, quantum pendulum dynamics holds sway.

We have begun what we hope will be a beginning of the study of wireless electrodynamic communication between biological cells starting with (say) bacteria or viruses that have DNA or RNA within the cell nucleus. The basic DNA and RNA microbe antennae must be wired in nature as a biological community of coherent phased antenna arrays for appreciable communication information bit-rates radiated through large distances. Arrays of biological weak links might serve that purpose.

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